Robust Latent Factor Analysis for Precise Representation of High-Dimensional and Sparse Data

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Abstract—High-dimensional and sparse (HiDS) matrices commonly arise in various industrial applications, e.g., recommender systems (RSs), social networks, and wireless sensor networks. Since they contain rich information, how to accurately represent them is of great significance. A latent factor (LF) model is one of the most popular and successful ways to address this issue. Current LF models mostly adopt L2-norm-oriented Loss to represent an HiDS matrix, i.e., they sum the errors between observed data and predicted ones with L_2 -norm. Yet L_2 -norm is sensitive to outlier data. Unfortunately, outlier data usually exist in such matrices. For example, an HiDS matrix from RSs commonly contains many outlier ratings due to some heedless/malicious users. To address this issue, this work proposes a smooth L₁-norm-oriented latent factor (SL-LF) model. Its main idea is to adopt smooth L_1 -norm rather than L_2 -norm to form its Loss, making it have both strong robustness and high accuracy in predicting the missing data of an HiDS matrix. Experimental results on eight HiDS matrices generated by industrial applications verify that the proposed SL-LF model not only is robust to the outlier data but also has significantly higher prediction accuracy than state-of-the-art models when they are used to predict the missing data of HiDS matrices.

Index Terms—High-dimensional and sparse matrix, L_1 -norm, L_2 -norm, latent factor model, recommender system, smooth L_1 -norm.

I. INTRODUCTION

I N this era of information explosion, people are frequently inundated by big data from various industrial applications [1]–[5], e.g., recommender systems (RSs), social networks, and wireless sensor networks. Among these applications, matrices are commonly adopted to represent the relationship between two types of entities. For example, a user-item rating

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matrix is frequently seen in recommender systems (RSs) [6]–[9], where each row indicates a specific user, each column indicates a specific item (e.g., movie, electronic product, and music), and each entry indicates a user's preference on an item.

In big data-related applications like Amazon [10], since the relation among numerous entities is unlikely to be fully observed in practice, matrices from these applications are usually high-dimensional and sparse (HiDS) [7], [11]. Yet these HiDS matrices contain rich formation regarding various valuable knowledge, e.g., user's potential preferences on items in RSs. Hence, how to precisely extract useful information from an HiDS matrix becomes a hot yet thorny issue in industrial applications.

Up to now, various approaches and models are proposed to address this issue [6]–[9]. Among them, a latent factor (LF) model, which originates from matrix factorization techniques [11], [12], is becoming increasingly popular due to its high accuracy and scalability in industrial applications [13], [14]. Given an HiDS matrix, an LF model represents it by training two low-dimensional LF matrices based on its observed data only [13], [15]. To model an accurate LF model, how to design its *Loss* function is very crucial, where *Loss* denotes the sum of errors between observed data (ground truths) and predicted ones computed by a specific norm on an HiDS matrix [13], [14].

Currently, most LF models adopt L_2 -norm-oriented Loss [12]–[18] while few ones adopt L_1 -norm-oriented Loss [19]. Fig. 1(a) illustrates the differences between L_1 -norm-oriented and L_2 -norm-oriented Losses [19]–[21] where Error denotes the errors between predicted results and ground truths: 1) the former is less sensitive to Error than the latter, thereby enhancing the robustness of a resultant model [19], [21], [22], and 2) the latter is smoother than the former when the absolute value of Error is small (less than 1), thereby enhancing the stability of a resultant model [23].

Hence, although an LF model with L_2 -norm-oriented Loss can achieve a steady and accurate prediction for the missing data of an HiDS matrix space [23], its robustness cannot be guaranteed when such a matrix is mixed with outlier data. Unfortunately, outlier data usually exist in an HiDS matrix. For example, an HiDS matrix from RSs commonly contains many outlier ratings due to some heedless/malicious users (e.g., a user rates an item randomly in the feedback or badmouths a specific item) [24], [25].

On the other hand, although an LF model with L_1 -normoriented *Loss* has intrinsic robustness, its solution space for predicting the missing data of an HiDS matrix is multimodal. The reason is that L_1 -norm-oriented *Loss* is not smooth when the predicted results and ground truths are close to each other. As a result, an LF model with L_1 -norm-oriented *Loss* may be stacked by some "bad" solutions, making it unable to guarantee high prediction accuracy.

From the aforementioned discussions, we see that both L_1 and L_2 -norm-oriented *Losses* are not the best choice for modeling an LF model. Then, do we have an alternative one? This work aims to answer it. Fig. 1(b) illustrates the smooth L_1 -norm-oriented *Loss*, where we observe that *Loss* not only is robust to *Error* but also has a smooth gradient when the absolute value of *Error* is smaller than 1. Motivated by this observation, we propose a smooth L_1 -norm-oriented latent factor (SL-LF) model. Its main idea is to adopt smooth L_1 norm to form its *Loss*, making it have both strong robustness and high accuracy in predicting the missing data of an HiDS matrix.

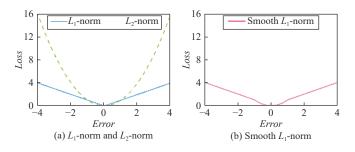


Fig. 1. The relationship between *Loss* and *Error* with different norms to solve a regression problem.

Main contributions of this work include:

1) Proposing an SL-LF model with strong robustness and high accuracy in predicting the missing data of an HiDS matrix.

2) Performing a suite of theoretical analyses and algorithm designs for the proposed SL-LF model.

3) Conducting extensive empirical studies on eight HiDS matrices generated by industrial applications to evaluate the proposed model and other state-of-the-art ones.

To the author's best knowledge, this is the first study to employ smooth L_1 -norm to implement an LF model for predicting the missing data of an HiDS matrix. Experimental results demonstrate that compared with state-of-the-art models, SL-LF achieves significant accuracy gain when predicting missing data of an HiDS matrix. Its computational efficiency is also highly competitive when compared with the most efficient LF models.

The rest of the paper is organized as follows. Section II states preliminaries. Section III presents an SL-LF model. Section IV reveals experimental results. Section V discusses related work. Finally, Section VI concludes this paper.

II. PRELIMINARIES

In this section, we give the related definitions and descriptions of an HiDS matrix and an LF model. According

to [9], [16], [18], they are defined as follows.

Definition 1 (HiDS matrix): Given a set U and a set I, Z denotes a $|U| \times |I|$ matrix where each element $z_{u,i}$ denotes the relation between element u ($u \in U$) and element i ($i \in I$). Z_K and Z_U respectively denote the known and the unknown entities sets of Z. Z is an HiDS matrix with $|Z_K| <<|Z_U|$.

Built on an HiDS matrix, an LF model is defined as follows [13], [14], [26].

Definition 2 (Latent factor model): Given Z, f, a $|U| \times f$ latent factor matrix X, and an $|I| \times f$ latent factor matrix Y, a latent factor model is to search for X and Y to achieve Z's rank-f approximation \widehat{Z} by minimizing the errors between Z and \widehat{Z} on Z_K with the condition of $f << \min\{|U|, |I|\}$, where \widehat{Z} is given by $\widehat{Z} = XY^T$. \widehat{Z} 's each element $\widehat{z}_{u,i}$ is the prediction for each $z_{u,i}$.

To implement an LF model, a *Loss* function needs to be carefully designed to measure the difference between Z and \widehat{Z} [14]. Currently, L_2 -norm is most commonly used [7], [17]:

$$\underset{X,Y}{\operatorname{arg\,min}} \varepsilon(X,Y) = \left\| \Omega \odot \left(Z - \widehat{Z} \right) \right\|_{L_2}^2 = \left\| \Omega \odot \left(Z - XY^T \right) \right\|_{L_2}^2 \quad (1)$$

where $\|\cdot\|_{L_2}$ denotes the L_2 -norm of a matrix, \odot denotes the Hadamard product (the component-wise multiplication), and Ω is $a |U| \times |I|$ binary index matrix:

$$\Omega_{u,i} = \begin{cases} 1, & \text{if } z_{u,i} \text{ is known} \\ 0, & \text{otherwise.} \end{cases}$$
(2)

As analyzed in [14], an LF model is easy to overfit on Z_K of an HiDS matrix by minimizing (1). Tikhonov regularization is thus adopted to prevent such an overfitting problem [9], [16], [18]. Then, with it, an LF model has the following objective function:

$$\underset{X,Y}{\operatorname{arg\,min}} \varepsilon(X,Y) = \left\| \Omega \odot \left(Z - XY^T \right) \right\|_{L_2}^2 + \lambda \left(\|X\|_{L_2}^2 + \|Y\|_{L_2}^2 \right) \quad (3)$$

where λ is a regularization controlling parameter. Next, we present an SL-LF model.

III. SMOOTH L1-NORM-ORIENTED LATENT FACTOR MODEL

A. Objective Formulation

As L_2 -norm is sensitive to outlier data [20], an LF model with a *Loss* function of (1) lacks robustness. On the other hand, an LF model with an L_1 -norm-oriented *Loss* function cannot guarantee a high prediction accuracy because its solution space is not smooth. As shown in Fig. 1(b), smooth L_1 -norm has the merits of both robustness and smoothness. Yet it remains open whether an LF model with a smooth L_1 norm-oriented *Loss* function can achieve a highly robust and accurate prediction for the missing data of an HiDS matrix. To answer it, we first define the smooth L_1 -norm of a matrix.

Definition 3 (Smooth L_1 -norm of a matrix): Given a matrix R with M rows and N columns, symbol $||R||_{SL_1}$ denotes the smooth L_1 -norm of R.

$$\|R\|_{SL_1} = \sum_{m=1}^{M} \sum_{n=1}^{N} v, \ v = \begin{cases} \sqrt{r_{m,n}^2}, & \text{if } |r_{mn}| \le 1\\ |r_{mn}|, & \text{if } |r_{mn}| > 1 \end{cases}$$
(4)

where $r_{m,n}$ denotes R's element at *m*-th row and *n*-th column,

 $m \in \{1, 2, ..., M\}, n \in \{1, 2, ..., N\}.$

Then, to implement an SL-LF model, we design the following objective function:

$$\underset{X,Y}{\operatorname{arg\,min}} \varepsilon(X,Y) = \left\| \Omega \odot \left(Z - XY^T \right) \right\|_{SL_1}^2 + \lambda \left(\|X\|_{L_2}^2 + \|Y\|_{L_2}^2 \right)$$
(5)

where $\|\cdot\|_{SL_1}$ denotes the smooth L_1 -norm of a matrix. As Z contains numerous unknown data, (5) should be expanded into the following data density-oriented form for high efficiency in both storage and computation [13], [15]:

$$\arg\min_{X,Y} \varepsilon(X,Y) = \left\{ \begin{array}{l} \sum_{(u,i)\in Z_K} \left(\Delta_{u,i} \right)^2 + \lambda \sum_{(u,i)\in Z_K} \left(\sum_{k=1}^f x_{u,k}^2 + \sum_{k=1}^f y_{i,k}^2 \right) \\ \text{if } \left| \Delta_{u,i} \right| \le 1 \\ \sum_{(u,i)\in Z_K} \left| \Delta_{u,i} \right| + \lambda \sum_{(u,i)\in Z_K} \left(\sum_{k=1}^f x_{u,k}^2 + \sum_{k=1}^f y_{i,k}^2 \right) \\ \text{if } \left| \Delta_{u,i} \right| > 1 \end{array} \right.$$
(6)

where $x_{u,k}$ denotes the specific entity at the *u*-th row and *k*-th column in *X*, $y_{i,k}$ denotes the specific entity at the *i*-th row and *k*-th column in *Y*, and $\Delta_{u,i}$ is the prediction error between $z_{u,i}$ and $\hat{z}_{u,i}$ calculated as

$$\Delta_{u,i} = z_{u,i} - \hat{z}_{u,i} = z_{u,i} - \sum_{k=1}^{J} x_{u,k} y_{i,k}.$$
 (7)

With such an objective function of (6), we next check whether an SL-LF model can achieve a highly robust and accurate prediction for the missing data of an HiDS matrix.

B. Model Optimization

As analyzed in [13], [15], a stochastic gradient descent (SGD) algorithm has the advantages of fast convergence and ease of implementation in optimizing a bilinear objective. Hence, we employ it to minimize (6) by training desired X and Y. First, we consider the instant loss of (6) on a single entity $z_{u,i}$.

$$\varepsilon_{u,i} = \begin{cases} \left(\Delta_{u,i} \right)^2 + \lambda \left(\sum_{k=1}^f x_{u,k}^2 + \sum_{k=1}^f y_{i,k}^2 \right), & \text{if } \left| \Delta_{u,i} \right| \le 1 \\ \left| \Delta_{u,i} \right| + \lambda \left(\sum_{k=1}^f x_{u,k}^2 + \sum_{k=1}^f y_{i,k}^2 \right), & \text{if } \left| \Delta_{u,i} \right| > 1. \end{cases}$$
(8)

To solve (8) with SGD, we need to respectively move each single LF $x_{u,k}$ and $y_{i,k}$ along the opposite of the stochastic gradient of (8). To do so, we make

$$\begin{cases} x_{u,k} = x_{u,k} - \eta \frac{\partial \varepsilon_{u,i}}{\partial x_{u,k}} \\ y_{i,k} = y_{i,k} - \eta \frac{\partial \varepsilon_{u,i}}{\partial y_{i,k}} \\ \forall k \in \{1, 2, ..., f\} \end{cases}$$
(9)

where η is the learning rate. Since (8) has the absolute deviation term of $|\Delta_{u,i}|$, there are a total of three situations for (8) in computing (9) as follows:

$$\varepsilon_{u,i} = \begin{cases} \left(\Delta_{u,i} \right)^2 + \lambda \left(\sum_{k=1}^{f} x_{u,k}^2 + \sum_{k=1}^{f} y_{i,k}^2 \right), & \text{if } |\Delta_{u,i}| \le 1 \\ \Delta_{u,i} + \lambda \left(\sum_{k=1}^{f} x_{u,k}^2 + \sum_{k=1}^{f} y_{i,k}^2 \right), & \text{if } \Delta_{u,i} > 1 \\ -\Delta_{u,i} + \lambda \left(\sum_{k=1}^{f} x_{u,k}^2 + \sum_{k=1}^{f} y_{i,k}^2 \right), & \text{if } \Delta_{u,i} < -1. \end{cases}$$
(10)

Then, by incorporating (10) into (9), we have the training rules for each single LF $x_{u,k}$ and $y_{i,k}$ respectively on a single entity $z_{u,i}$ as follows:

For
$$z_{u,i} \quad \forall k \in \{1, 2, ..., f\}$$
:

$$\begin{cases}
x_{u,k} = x_{u,k} + \eta y_{i,k} \varDelta_{u,i} - \eta \lambda x_{u,k}, & \text{if } |\varDelta_{u,i}| \leq 1 \\
y_{i,k} = y_{i,k} + \eta x_{u,k} \varDelta_{u,i} - \eta \lambda y_{i,k}, & \text{if } \varDelta_{u,i} > 1 \\
y_{i,k} = y_{i,k} + \eta x_{u,k} - \eta \lambda y_{i,k}, & \text{if } \varDelta_{u,i} > 1 \\
x_{u,k} = x_{u,k} - \eta y_{i,k} - \eta \lambda x_{u,k}, & \text{if } \varDelta_{u,i} < -1. \\
y_{i,k} = y_{i,k} - \eta x_{u,k} - \eta \lambda y_{i,k}, & \text{if } \varDelta_{u,i} < -1.
\end{cases}$$

After all the known entities in Z_K are employed to train by (11), we get the desired X and Y. Finally, Z's rank-f approximation \widehat{Z} , which can predict the missing data of Z, is obtained as $\widehat{Z} = XY^T$.

C. Incorporating Linear Biases into SL-LF

According to [14], [27], [28], linear biases can be incorporated into an LF model to improve its prediction accuracy. Since SL-LF is also an LF-based model, we can extend it with linear biases. As analyzed in [14], [27], [28], linear biases commonly include the global average and the observed deviations on users and items. With them, then, an SL-LF model approximates $\hat{z}_{u,i}$ as follows:

$$\hat{z}_{u,i} = \mu + b_u + b_i + \sum_{k=1}^{f} x_{u,k} y_{i,k}$$
(12)

where μ denotes the global average value in Z_K , b_u denotes the observed deviations on user u, and b_i denotes the observed deviations on item i, respectively. Given an HiDS matrix Z, μ is computed as follows:

$$\mu = \frac{\sum_{(u,i)\in Z_K} r_{u,i}}{|Z_K|}.$$
(13)

After that, b_u and b_i can be estimated in an easy way [27], [28]:

$$b_{i} = \frac{\sum_{(u,i)\in Z(i)} (r_{u,i} - \mu)}{\theta_{1} + |Z(i)|}, \ b_{u} = \frac{\sum_{(u,i)\in Z(u)} (r_{u,i} - \mu - b_{i})}{\theta_{2} + |Z(u)|}$$
(14)

where Z(i) denotes the known entities set in the *i*-th column of *Z*, Z(u) denotes the known entities set in the *u*-th row of *Z*, θ_1

799

and θ_2 denote the threshold constant and can be determined by cross-validation [28]. Then, by incorporating linear biases into SL-LF, (7) is changed into:

$$\Delta_{u,i} = z_{u,i} - \hat{z}_{u,i} = z_{u,i} - \mu - b_u - b_i - \sum_{k=1}^f x_{u,k} y_{i,k}.$$
 (15)

Finally, by combining (15) into (11), we can obtain the training rules for SL-LF with linear biases on a single entity $z_{\mu,i}$.

D. Algorithm Design and Analysis

From the above analyses, we see that SL-LF has two versions, i.e., without and with linear biases. We respectively name SL-LF without and with linear biases as $SL-LF_{\bar{b}}$ and $SL-LF_{\bar{b}}$. First, we design Algorithm 1 for $SL-LF_{\bar{b}}$, whose computational complexity $C_{\bar{b}}$ can be derived as follows:

$$C_{\bar{b}} = \Theta(1) + \Theta(|U| \times f) + \Theta(|I| \times f) + N_{mtr} \times (|Z_K| \times f \times 2 \times \Theta(1) + \Theta(1)) \approx \Theta(N_{mtr} \times |Z_K| \times f)$$
(16)

where we drop the lower order terms due to $(|U| + |I|) << |Z_K|$ in real-world applications. Second, we design Algorithm 2 for SL-LF_b, whose computational complexity C_b can be derived as follows:

$$C_{b} = \Theta(1) + \Theta(|U| \times f) + \Theta(|I| \times f) + \Theta(|Z_{K}|) + \Theta(|Z_{K}|) + \Theta(|Z_{K}|) + N_{mtr} \times (|Z_{K}| \times f \times 2 \times \Theta(1) + \Theta(1)) \approx \Theta(N_{mtr} \times |Z_{K}| \times f).$$
(17)

From (16) and (17), we see that SL-LF_b and SL-LF_b have the same computational complexity. The maximal-traininground count N_{mtr} , known entity count $|Z_K|$, and LF space dimension f are crucial in deciding their computational complexity.

Besides, to implement SL-LF_b, we need the following data structures: 1) two arrays with length $|Z_K|$ to cache training data and corresponding predictions, 2) an array with length |U| to cache observed deviations on users, 3) an array with length |I| to cache observed deviations on items, 4) a matrix with size $|U| \times f$ to cache X, and 5) a matrix with size $|I| \times f$ to cache Y. Thus, SL-LF_b's space complexity is

$$S_B = 2|Z_K| + |U| + |I| + |U| \times f + |I| \times f$$

$$\approx \Theta\left(f \times \max\left\{\frac{|Z_K|}{f}, |U|, |I|\right\}\right).$$
(18)

Although SL-LF_b does not need arrays to cache linear biases, it has the same space complexity as SL-LF_b.

In real-world applications, both N_{mtr} and f are positive constants. Hence, SL-LF's computational and space complexity is linear with $|Z_K|$, which is highly efficient and applicable to big data-related industrial applications.

IV. EXPERIMENTS AND RESULTS

A. General Settings

Datasets: Eight benchmark datasets are selected to conduct the experiments. Table I summarizes their properties. They are real HiDS datasets generated by industrial applications and frequently adopted by prior studies [13], [29]. Dating is collected by an online dating website LibimSeTi [30], Douban is collected by Douban.com [13], [29], Eachmovie is collected by the EachMovie system by the DEC Systems Research Center [1], [31], Epinion is collected by Trustlet website [29], Flixter is collected by the Flixter website [32], Jester is collected by the joke-recommender Jester [32], and MovieLens_10M and MovieLens_20M are collected by the MovieLens system [33].

Algorithm 1 S	L-LF _b
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Input: Z_{κ}	
Operation \mathcal{L}_{K}	Cost
initializing $f, \lambda, \eta, Nmtr$ (Max-training-round count)	$\Theta(1)$
initializing X randomly	$\Theta(U \times f)$
initializing Y randomly	$\Theta(I \times f)$
while $t \leq Nmtr$ && not converge	×Nmtr
for each entity $z_{u,i}$ in Z_K	$\times Z_K $
for <i>k</i> =1 to <i>f</i>	$\times f$
computing $x_{u,k}$ according to (7) and (11)	$\Theta(1)$
computing $y_{i,k}$ according to (7) and (11)	$\Theta(1)$
end for	-
end for	-
t=t+1	$\Theta(1)$
end while	-
Output: X, Y	

Algorithm 2 SL-LF_b

Input: Z _K	
Operation	Cost
initializing f, λ, η , Nmtr (Max-training-round count)	$\Theta(1)$
initializing X randomly	$\Theta(U \times f)$
initializing Y randomly	$\Theta(I \times f)$
computing μ according to (13)	$\Theta(Z_K)$
for each entity $z_{u,i}$ in Z_K	$\times Z_K $
computing b_i according to (14)	$\Theta(1)$
end for	-
for each entity $z_{u,i}$ in Z_K	$\times Z_K $
computing b_u according to (14)	$\Theta(1)$
end for	-
while $t \le Nmtr$ && not converge	×Nmtr
for each entity $z_{u,i}$ in Z_K	$\times Z_K $
for $k=1$ to f	$\times f$
computing $x_{u,k}$ according to (11) and (15)	$\Theta(1)$
computing $y_{i,k}$ according to (11) and (15)	Θ(1)
end for	-
end for	-
<i>t</i> = <i>t</i> +1	$\Theta(1)$
end while	-
Output: X, Y	

Evaluation Metrics: Missing data prediction is a common but important task in representing an HiDS matrix [34]. To evaluate prediction accuracy, mean absolute error (MAE) and root mean squared error (RMSE) are widely adopted:

$$MAE = \left(\sum_{(u,i)\in\Gamma} \left|z_{u,i} - \hat{z}_{u,i}\right|_{abs}\right) / |\Gamma|$$

TABLE I PROPERTIES OF ALL THE DATASETS

No.	Name	U	I	$ Z_K $	Density
D1	Dating	135 359	168 791	17 359 346	0.08%
D2	Douban	129 490	58 541	16 830 839	0.22%
D3	Eachmovie	72 916	1 628	2 811 718	2.37%
D4	Epinion	755 760	120 492	13 668 321	0.02%
D5	Flixter	147 612	48 794	8 196 077	0.11%
D6	Jester	24 983	100	1 186 324	47.49%
D7	MovieLens_10M	71 567	65 133	10 000 054	0.21%
D8	MovieLens_20M	138 493	26 744	20 000 263	0.54%

$$RMSE = \sqrt{\left(\sum_{(u,i)\in\Gamma} (z_{u,i} - \hat{z}_{u,i})^2\right)/|\Gamma|}$$

where Γ denotes the testing set and $|\cdot|_{abs}$ denotes the absolute value of a given number. Lower MAE and RMSE indicate higher missing data prediction accuracy. Besides, to evaluate the computational efficiency of missing data prediction, we measure CPU running time.

Experimental Designs: For each dataset, its 80% known data are used as a training dataset and the remaining 20% ones as a testing dataset. Five-fold cross-validations are adopted. All the experiments are run on a PC with 3.4 GHz i7 CPU and 64 GB RAM. In the next experiments, we aim at answering the following research questions:

1) How do the hyper-parameters of an SL-LF model impact its prediction performance?

2) How do the outlier data impact the prediction performance of an SL-LF model?

3) Does the proposed SL-LF model outperform related state-of-the-art models?

B. Hyper-Parameter Sensitivity Tests

From Section III, we know that SL-LF has three parameters, i.e., LF space dimension *f*, regularization parameter λ , and learning rate η . Next, we analyze the behaviors of SL-LF_b (without linear biases) and SL-LF_b (with linear biases) with respect to these parameters.

1) Impacts Off

This set of experiments increase f from 5 to 320. Figs. 2 and 3 record the results on D8. The complete results on all the datasets are recorded in the Supplementary File¹ of this paper. From these results, we find that the larger f makes both SL- $LF_{\bar{b}}$ and $SL-LF_{b}$ have better representation learning ability on most cases, which benefits for achieving a higher prediction accuracy. However, such prediction accuracy gain slows down when f is larger than a threshold, such as 20. Moreover, we find exceptions that prediction accuracy decreases when f increases from 5 to 40 on D4. One reason may be that underfitting is caused by such hyper-parameters. Besides, the larger f requires more computational cost as analyzed in (16) and (17). Hence, f should be set appropriately to balance prediction accuracy and computational cost according to a specific task. As a rule of thumb, f is usually set to fall into 10-20 [14], [15], [35].

¹https://pan.baidu.com/s/10_8sKP0HRluNH1a4IWHW8w, Code: t3sw

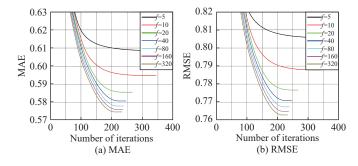


Fig. 2. The training process of SL-LF_b with different *f* on D8, where $\lambda = 0.01$ and $\eta = 0.001$.

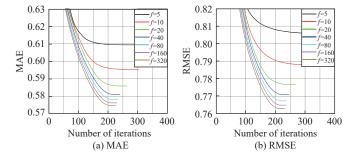


Fig. 3. The training process of SL-LF_b with different f on D8, where $\lambda = 0.01$ and $\eta = 0.001$.

2) Impacts of λ and η

In this set of experiments, we increase λ from 0.01 to 0.1 and η from 0.0001 to 0.01 by performing a grid-based search [36]. Figs. 4 and 5 show the results on D8. The complete results on all the datasets are presented in the Supplementary File¹. From them, we conclude that:

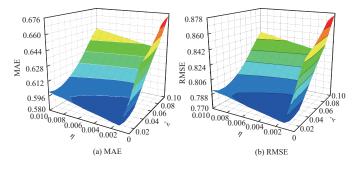


Fig. 4. The experimental results of SL-LF_b with respect to λ and η on D8, where f = 20.

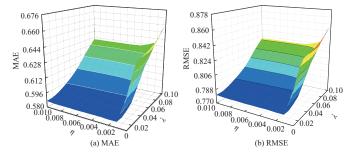


Fig. 5. The experimental results of SL-LF_b with respect to λ and η on D8, where f = 20.

TABLE II DESCRIPTIONS OF ALL THE COMPARISON MODELS

Model	Description
BLF	The basic LF model proposed in 2009 [14]. It has been extensively used in RSs.
NLF	The regularized non-negative LF model proposed in 2016 [15]. It improves the L2-LF model by introducing the non-negative constraint into objective function design.
FNLF	A fast non-negative LF model based on generalized momentum proposed in 2018 [7]. It improves the NLF model.
AutoRec	A DNN-based model proposed in 2015 [37]. It is an autoencoder [38] framework for CF. It is a representative model in DNN-based RSs.
DCCR	A DNN-based model proposed in 2019 [39]. It improves AutoRec by using two different neural networks.
SL-LF _b	The proposed SL-LF model without linear biases.
SL-LF _b	The proposed SL-LF model with linear biases.

a) Both λ and η have a significant impact on prediction accuracy of both SL-LF_b and SL-LF_b. As λ and η increase, MAE and RMSE decrease at first and then increase in general. For example, on D8, RMSE of SL-LF_b decreases from 0.8116 to 0.7729 at the beginning. Then, it increases up to 0.8451 as λ and η continue to increase.

b) λ and η have different situations in searching their optimal values on the tested datasets. On the different datasets, the optimal value of η is a small value like 0.001. However, the optimal value of λ is different for the different datasets. It distributes in the range from 0.02 to 0.09. Hence, λ should be carefully tuned on the target dataset.

C. Outlier Data Sensitivity Tests

In this section, we compare an SL-LF model with a basic LF (BLF) model when outlier data are added to the datasets. BLF is modeled based on the L_2 -norm-oriented *Loss* while SL-LF is done by the smooth L_1 -norm-oriented *Loss*. The specific method of adding outlier data is: 1) randomly selecting an unknown entity between two known entities as the outlier entity for the input HiDS matrix *Z*, 2) assigning a value (maximum or minimum known value) to the outlier entity, 3) the percentage that outlier entities account for known entities is increased from 0% to 100% with an interval of 10%, and 4) the outlier entities are only added into the training set. To illustrate this method, an example is given in Fig. 6.



Fig. 6. An example of adding outlier data.

Fig. 7 records the experimental results on D8. Supplementary File¹ records the complete results on all the datasets. Since smooth L_1 -norm is less sensitive to outlier data than L_2 -norm, we find that both SL-LF_b and SL-LF_b become much more robust than BLF as the percentage of outlier data increases. For example, on D8, RMSEs of SL-LF_b and BLF are 0.7767 and 0.7761, respectively when there are no outlier data, and then become 0.8536 and 1.1244, respectively when the percentage of outlier data is 100%. The improvement of RMSE of BLF is 0.3483, which is about 4.53 times as large as that of SL-LF_b at 0.0769. Therefore, we conclude that an SL-LF model is robust to the outlier data.

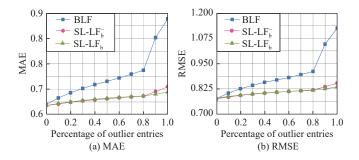


Fig. 7. The outlier data sensitivity tests results of BLF, SL-LF_b, and SL-LF_b on D8, where $\lambda = 0.01$, $\eta = 0.001$, and f = 20.

D. Comparison Between SL-LF and State-of-the-Art Models

We compare an SL-LF model with five related state-of-theart models, including three LF-based models (basic latent factor (BLF), non-negative latent factor (NLF), and fast nonnegative latent factor (FNLF)) and two deep neural network (DNN)-based models (AutoRec and deep collaborative conjunctive recommender (DCCR)). Table II gives a brief introduction to these models. To make a fair comparison, f is set as 20 for all the LF-based models and the proposed SL-LF model. Besides, we tune the other hyper-parameters for all the involved models to make them achieve their highest prediction accuracy.

1) Comparison of Prediction Accuracy

Table III presents the detailed comparison results. Statistical analysis is conducted on these comparison results. First, the win/loss counts of SL-LF_b/SL-LF_b versus other models are summarized in the third/second-to-last row of Table III. Second, we perform Friedman test [40] on these comparison results. The result is recorded in the last row of Table III, where it accepts the hypothesis that these comparison models have significant differences with a significance level of 0.05. From these comparisons and statistical results, we find that a) both SL-LF_b and SL-LF_b achieve lower RMSE/MAE than the other models on most testing cases, and b) SL-LF_b achieves the lowest F-rank value among all the models. Hence, we conclude that SL-LF_b has the highest prediction accuracy

TABLE III
THE COMPARISON RESULTS ON PREDICTION ACCURACY, INCLUDING WIN/LOSS COUNTS STATISTIC AND FRIEDMAN TEST, WHERE • AND Respectively Indicate That SL-LF _b , and SL-LF _b Have a Higher Prediction Accuracy Than Comparison Models
Respectively indicate that SL -LF _b , and SL -LF _b have a higher prediction accuracy than comparison models

Dataset	Metric	BLF	NLF	FNLF	AutoRec	DCCR	$SL-LF_{\bar{b}}$	SL-LF
51	MAE	1.2392•۞	1.2617• 🛇	1.2588• 🛇	1.2610•۞	1.2574• 🗘	1.1702	1.1686
D1	RMSE	1.8066 🛇	1.8245 🛇	1.8215 🛇	1.8027 🛇	1.8013 🛇	1.8275	1.7829
50	MAE	0.5537•۞	0.5590• 😋	0.5592• 😋	0.5606•۞	0.5581•😋	0.5516	0.5458
D2	RMSE	0.7139•۞	0.7150• 🛇	0.7139• 🛇	0.7080 🛇	0.7074 🛇	0.7094	0.6957
D	MAE	0.1732•۞	0.1767•۞	0.1763•۞	0.1784•۞	0.1775•۞	0.1731	0.1729
D3	RMSE	0.2251•	0.2264• 😋	0.2259•	0.2305••	0.2289• 😂	0.2242	0.2260
	MAE	0.3011•😋	0.3047• 🛇	0.3036• 🛇	0.3014• 🛇	0.3036• 😂	0.2967	0.276
D4	RMSE	0.5958 😋	0.5994• 🛇	0.5977 😋	0.5946 😋	0.5952 😋	0.5992	0.4812
	MAE	0.6447•😋	0.6550• 😋	0.6520• 😋	0.6295 😋	0.6308 😂	0.6348	0.6084
D5	RMSE	0.8961•😋	0.9056• 😋	0.9038• 😋	0.8682 😋	0.8792 🛇	0.8949	0.8324
-	MAE	0.7664•😋	0.7769• 😂	0.7778• 😋	0.7905•😋	0.7883•۞	0.7552	0.7573
D6	RMSE	0.9957 😋	1.0049•😋	1.0003•۞	1.0078•۞	1.0042•😂	0.9988	0.993
77	MAE	0.5999• 🗘	0.6080• 😋	0.6068• 😋	0.6048•😋	0.6002•😂	0.5950	0.5980
D7	RMSE	0.7819•	0.7893•۞	0.7881•	0.7865•	0.7847•	0.7806	0.7887
Dû	MAE	0.5886• 😂	0.5977• 😂	0.5961•😋	0.5947•😋	0.5902• 😂	0.5841	0.5857
D8	RMSE	0.7737•	0.7819• 😋	0.7798• 😋	0.7802•😋	0.7789•	0.7730	0.7790
	• Win/Loss	13/3	15/1	14/2	11/5	11/5	_	_
Statistical analysis	Win/Loss	13/3	16/0	14/2	15/1	14/2	_	-
	F-rank*	3.281	6.313	5.125	4.813	3.969	2.625	1.875

* The smaller F-rank value denotes a higher prediction accuracy.

among all the models.

Next, we check whether SL-LF_b achieves significantly higher prediction accuracy than each single model. To do so, we conduct the Wilcoxon signed-ranks test [41], [42] on the comparison results of Table III. Wilcoxon signed-ranks test is a nonparametric pairwise comparison procedure and has three indicators – R+, R–, and p-value. The larger R+ value indicates higher performance and the p-value indicates the significance level. Table IV records the test results, where we see that SL-LF_b has a significantly higher prediction accuracy than all the comparison models with a significance level of 0.05 except for SL-LF_b. However, SL-LF_b achieves a much larger R+ value than SL-LF_b, which verifies that linear biases can boost an SL-LF model's prediction accuracy.

2) Comparison of Computational Efficiency

To compare the computational efficiency of all the tested models, we measure their CPU running times on all the datasets. Fig. 8 presents the results. From it, we observe that:

a) DNN-based models (AutoRec and DCCR) cost much more CPU running time than the other models due to their time-consuming DNN-based learning strategy [43].

b) SL-LF costs slightly more CPU running time than BLF. The reason is that SL-LF has the additional computational procedures of discrimination (11) while BLF does not.

c) SL-LF costs less or more CPU running time than NLF and FNLF on the different datasets.

Therefore, these results verify that SL-LF's computational efficiency is higher than those of DNN-based models and comparable to those of other LF-based models.

TABLE IV STATISTICAL RESULTS ON TABLE III BY CONDUCTING THE WILCOXON SIGNED-RANKS TEST

Comparison	R+	R-	<i>p</i> -Value
SL-LF _b vs. BLF	121	15	0.0033
SL-LF _b vs. NLF	136	0	0.0002
SL-LF _b vs. FNL	133	3	0.0004
SL-LF _b vs. AutoRec	134	2	0.0004
SL-LF _b vs. DCCR	131	5	0.0006
$\text{SL-LF}_{\rm b}$ vs. $\text{SL-LF}_{\rm \bar{b}}$	100	37	0.0544

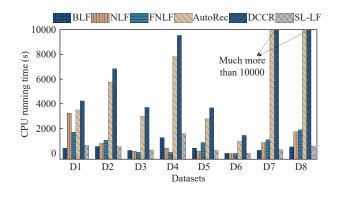


Fig. 8. The comparison CPU running time of involved models on D1-D8.

E. Summary of Experiments

Based on the above experimental results and analyses, we have the following conclusions:

1) An SL-LF model's prediction accuracy is closely connected with λ and η . As a rule of thumb, we can set η =0.001 while λ should be fine-tuned according to a specific target dataset.

2) SL-LF has significantly higher prediction accuracy than state-of-the-art models for the missing data of an HiDS matrix.

3) SL-LF's computational efficiency is much higher than those of DNN-based models and comparable to those of most efficient LF-based models.

 Linear biases have positive effects on improving SL-LF's prediction accuracy.

V. RELATED WORK

An LF model is one of the most popular and successful ways to efficiently predict the missing data of an HiDS matrix [13], [14]. Up to now, various approaches are proposed to implement an LF model, including a bias-based one [14], non-negativity-constrained one [15], randomized one [17], probabilistic one [44], dual-regularization-based one [45], posterior-neighborhood-regularized one [16], graph regularized one [18], neighborhood-and-location integrated one [6], data characteristic-aware one [35], confidence-driven one [46], deep-latent-factor based one [47], and nonparametric one [48]. Although they are different from one another in terms of model design or learning algorithms, they all adopt an L_2 -norm-oriented *Loss*, making them sensitive to outlier data [20]. Since outlier data are frequently found in an HiDS matrix [24], [25], their robustness cannot be guaranteed.

To make an LF model less sensitive to outlier data, Zhu *et al.* [19] proposed to adopt an L_1 -norm-oriented *Loss*. However, such an LF model is multimodal because L_1 norm is less smooth than L_2 norm, as shown in Fig. 1(a). Hence, an LF model with an L_1 norm-oriented *Loss* tends to be stacked by some "bad" solutions, resulting in its failure to achieve high prediction accuracy. Differently from these approaches, the proposed SL-LF model adopts smooth L_1 -norm-oriented *Loss*, making its solution space smoother and less multimodal than that of an LF model with L_1 norm-oriented *Loss*. Meanwhile, its robustness is also higher than that of an LF model with L_2 norm-oriented *Loss*.

Recently, DNN-based approaches to represent an HiDS matrix have attracted extensive attention [49]. According to a recent review regarding DNN-based studies [34], various models are proposed to address the task of missing data prediction for an HiDS matrix. Representative models include an autoencoder-based model [37], hybrid autoencoder-based model [39], multitask learning framework [50], neural factorization machine [51], attentional factorization machine [52], deep cooperative neural network [53], and convolutional matrix factorization model [54]. However, DNN-based models have the limit of high computational cost caused by their learning strategies. For example, they take complete data rather than known data of an HiDS matrix as input. Unfortunately, an HiDS matrix generated by RSs commonly has a very low rating density. In comparison, SL-LF trains only on the known data of an HiDS matrix, thereby achieving highly computational efficiency.

As analyzed in [13], [16], an LF model can not only predict the missing data of an HiDS matrix but also be used as a data representation approach. Hence, SL-LF has some potential applications in representation learning, such as community detection, autonomous vehicles [5], and medical image analysis [55]–[57]. Besides, some researchers incorporate non-negative constraints into an LF model to improve its performance [17]. Similarly, we plan to improve SL-LF by considering non-negative constraints [58] in the future.

VI. CONCLUSIONS

This study proposes, for the first time, a smooth L_1 -normoriented latent factor (SL-LF) model to robustly and accurately predict the missing data of a high-dimensional and sparse (HiDS) matrix. Its main idea is to employ smooth L_1 norm rather than L_2 -norm to form its Loss (the error between observed data and predicted ones), making it achieve highly robust and accurate prediction of missing data in a matrix. Extensive experiments on eight HiDS matrices from industrial applications are conducted to evaluate the proposed model. The experimental results verify that 1) it is robust to the outlier data, 2) it significantly outperforms state-of-the-art models in terms of prediction accuracy for the missing data of an HiDS matrix, and 3) its computational efficiency is much higher than those of DNN-based models and comparable to those of most efficient LF models. Although it has shown promising prospects, how to make its hyper-parameter λ selfadaptive and improve its performance by considering nonnegative constraint remains open. We plan to fully investigate these issues in the future.

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